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Study of the inner dust envelope and stellar photosphere of the AGB star R Doradus using SPHERE/ZIMPOL

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ABSTRACT

Context. On the asymptotic giant branch (AGB) low- and intermediate-mass stars eject a large fraction of their envelope, but the mechanism driving these outflows is still poorly understood. For oxygen-rich AGB stars, the wind is thought to be driven by radiation pressure caused by scattering of radiation off dust grains.

Aims. We study the photosphere, the warm molecular layer, and the inner wind of the close-by oxygen-rich AGB star R Doradus. We focus on investigating the spatial distribution of the dust grains that scatter light and whether these grains can be responsible for driving the outflow of this star.

Methods. We use high-angular-resolution images obtained with SPHERE/ZIMPOL to study R Dor and its inner envelope in a novel way. We present observations in filters V , $\text{cntH}\alpha$, and cnt820 and investigate the surface brightness distribution of the star and of the polarised light produced in the inner envelope. Thanks to second-epoch observations in $\text{cntH}\alpha$, we are able to see variability on the stellar photosphere. We study the polarised-light data using a continuum-radiative-transfer code that accounts for direction-dependent scattering of photons off dust grains.

Results. We find that in the first epoch the surface brightness of R Dor is asymmetric in V and $\text{cntH}\alpha$, the filters where molecular opacity is stronger, while in cnt820 the surface brightness is closer to being axisymmetric. The second-epoch observations in $\text{cntH}\alpha$ show that the morphology of R Dor has changed completely in a timespan of 48 days to a more axisymmetric and compact configuration. This variable morphology is probably linked to changes in the opacity provided by TiO molecules in the extended atmosphere. The observations show polarised light coming from a region around the central star. The inner radius of the region from where polarised light is seen varies only by a small amount with azimuth. The value of the polarised intensity, however, varies by between a factor of 2.3 and 3.7 with azimuth for the different images. We fit the radial profile of the polarised intensity using a spherically symmetric model and a parametric description of the dust density profile, $\rho(r) = \rho_0 r^{-n}$. On average, we find exponents of -4.5 ± 0.5 that correspond to a much steeper density profile than that of a wind expanding at constant velocity. The dust densities we derive imply an upper limit for the dust-to-gas ratio of $\sim 2 \times 10^{-4}$ at $5.0 R_*$. Considering all the uncertainties in observations and models, this value is consistent with the minimum values required by wind-driving models for the onset of a wind, of $\sim 3.3 \times 10^{-4}$. However, if the steep density profile we find extends to larger distances from the star, the dust-to-gas ratio will quickly become too small for the wind of R Dor to be driven by the grains that produce the scattered light.

Key words. techniques: polarimetric – stars: AGB and post-AGB – stars: individual: R Doradus – stars: winds, outflows – stars: imaging – stars: mass-loss

1. Introduction

The asymptotic giant branch (AGB) is one of the final stages of the evolution of low- and intermediate-mass stars, when a slow and dense outflow develops (Habing & Olofsson 2003). The wind is thought to be driven by radiation pressure on dust grains that can only form because pulsations enhance the density-scale-height of the stellar atmospheres. For oxygen-rich AGB stars

(where the carbon-to-oxygen ratio is lower than one), it has been proposed that large, translucent dust grains provide the required opacity and drive the wind through scattering of photons (Höfner 2008). However, many intricacies of the formation and processing of the oxygen-rich dust grains remain poorly constrained from observations. The translucent nature of these grains implies that they are not expected to produce significant infrared emission and, hence, most likely cannot be identified from infrared

spectra. The best way to study such grains is through the scattered stellar light they are expected to produce.

To advance our understanding of the AGB mass loss, we use high-angular-resolution observations acquired with SPHERE/ZIMPOL (Beuzit et al. 2008) on the Very Large Telescope (VLT) to investigate light polarised through scattering off dust grains in the inner wind of the AGB star R Doradus. This oxygen-rich star with spectral type M8 has a large angular diameter in the sky (≈ 57 mas) and a relatively low mass-loss rate, between 0.9 and $2.0 \times 10^{-7} M_{\odot} \text{ yr}^{-1}$ (Olofsson et al. 2002; Maercker et al. 2008; Khouri 2014). Its pulsation properties switch between one mode with a period of 332 days and $\Delta V = 1.5$ mag, and another with a period of 175 days and $\Delta V < 1$ mag (Bedding et al. 1998). Polarised light from a region very close to the star ($\approx 1.5 R_{\star}$) has been recently detected using NACO (Norris et al. 2012). The authors found that a model with grain radii of $0.3 \mu\text{m}$ and an inner radius of the dust envelope of 43.3 mas gives the best fit to the data.

2. Observations

2.1. Data acquisition and data reduction

R Dor was observed with ZIMPOL during the SPHERE science verification time using three filters, V , $\text{cntH}\alpha$, and cnt820 . The observations were taken in two epochs, 10 and 11 of December 2014 (V , $\text{cntH}\alpha$, and cnt820) and 28 of January 2015 ($\text{cntH}\alpha$). The total integration times for each filter and epoch are given in Table 1. Observations using filter cnt820 were done both with and without a neutral density (ND) filter. In the images obtained without the ND filter, the star saturated the detector. When the first-epoch $\text{cntH}\alpha$ images were taken the seeing was too high ($> 1.2''$) for an optimal behaviour of the instrument, therefore these data have to be interpreted with care.

The observations of R Dor resulted in individual data cubes, containing the frames recorded with the two cameras of the instrument (both equipped with the same filter). We processed these cubes individually using the data reduction pipeline of the instrument, in its pre-release version 0.14.0¹. Each cube produced Stokes $+Q$, $-Q$, $+U$ and $-U$ frames for the two cameras, together with intensity frames I_Q and I_U . We then aligned and de-rotated the resulting average frames using custom python routines. We adopt a pixel scale of $3.602 \pm 0.011 \text{ mas pix}^{-1}$ and a position angle of the vertical axis with respect to north of $357.95 \pm 0.55 \text{ deg}$ (Ch. Ginski, in prep.). Recently, new direction-dependent corrections to the pixel scale of less than 0.5% have been determined (see Ginski et al., in prep.). Since these are much smaller than the uncertainties from choosing the central pixel (see Sect. 3.2) for the region we consider, we have not included them.

We deconvolved the total intensity images (only) using the Lucy-Richardson (L-R) algorithm implemented in the IRAF² software package. The point-spread function (PSF) reference images of ψ^2 Ori were taken on the night of 31 March 2015, under comparable seeing conditions ($\sigma = 0.9''$) as the R Dor observations. For the cnt820 filter, we adopted the PSF observation in the TiO717 filter (with $\lambda_0 = 716.8 \mu\text{m}$ and $\Delta\lambda = 19.7 \mu\text{m}$) as no other PSF observation in the cnt820 filter was available. We stopped the L-R deconvolution after 80 iterations, as the deconvolved images do not show a significant evolution in additional processing steps. Since the PSF images were not acquired

simultaneously to the images of R Dor, we only show the deconvolved images to illustrate what the underlying source morphology might be. All the quantities that we present and model were extracted from the observed images and not from the deconvolved ones.

2.2. Observational results

2.2.1. The stellar photosphere

We first discuss the total intensity (Stokes I) images. The high spatial resolution achieved with SPHERE/ZIMPOL (≈ 20 mas) allows us to resolve the stellar disc of R Dor in the total intensity images (Figs. 1 and 2). The images acquired in the first epoch reveal a very asymmetrical source, with a horseshoe-shaped morphology both in V and in $\text{cntH}\alpha$. In these images, more emission arises from the northern hemisphere and there is a region of low surface brightness in the south-west. We find an azimuthally-averaged full-width at half maximum (FWHM) in V and $\text{cntH}\alpha$ in this epoch of ≈ 71 mas (see Table 1). This asymmetric morphology is not as prominent in the cnt820 images and the source is also smaller at this wavelength, with $\text{FWHM} \approx 58.3$ mas.

The surface brightness distribution of R Dor in $\text{cntH}\alpha$ changes between the two epochs of observation (Fig. 2). In January 2015, emission is concentrated in the central region and the intensity distribution is more axisymmetric, different from what is seen in the first epoch. In the second epoch the disc of R Dor has a $\text{FWHM} \approx 59.4$ mas in $\text{cntH}\alpha$. For reference, the 48 days that separate the two epochs correspond to slightly more than one-fourth of the shortest pulsation period of R Dor (175 days).

The values of the FWHM measured in the second epoch in filters cnt820 and $\text{cntH}\alpha$ are comparable to the stellar radius for a uniform disc obtained by Norris et al. (2012) of ≈ 27.2 mas, from observations that probe the stellar continuum in the near-infrared. However, the values of the FWHM in the first epoch in V and in $\text{cntH}\alpha$ are significantly larger than that (see Table 1).

A strong dependence of the size of the stellar disc on wavelength is a known feature of AGB stars. For instance, the measured uniform-disc diameters in the near-infrared is found to correlate with molecular spectral bands of CO and H₂O (see, e.g., Wittkowski et al. 2008; Woodruff et al. 2009). In the visible wavelength range, TiO is expected to be the main source of opacity for a late-type M star as R Dor. This molecule is found to dominate the spectrum in the wavelength range of V and $\text{cntH}\alpha$, but its opacity is lower in the wavelength range of filter cnt820 . For comparison, molecular contribution is expected to be very small in the wavelengths that Norris et al. performed their observations. For examples of spectra of late-type stars with band identification, see, e.g., Lançon & Wood (2000).

Jacob et al. (1997) measured the diameter of R Dor in the pseudo-continuum region around $0.82 \mu\text{m}$ and in a TiO absorption band at $0.85 \mu\text{m}$ and found the stellar diameter to be 20% larger in the TiO band. Follow-up observations (Jacob et al. 2004) between $0.65 \mu\text{m}$ and $0.99 \mu\text{m}$ confirmed that the stellar disc size increases in the TiO bands. Ireland et al. (2004) found asymmetries in the stellar disc of R Dor in the same wavelength range observed by Jacob et al. (2004). The authors, however, could not determine whether these asymmetries were caused by variations in molecular excitation or in the light scattered by dust grains. Since we find that the size and the morphology of the stellar disc change considerably while the polarisation degree does not decrease significantly (see Sect. 2.2.2), we conclude that the difference in FWHM, the asymmetries, and the variation in

¹ Downloadable from <ftp://ftp.eso.org/pub/dfs/pipelines/sphere/>

² <http://iraf.noao.edu>

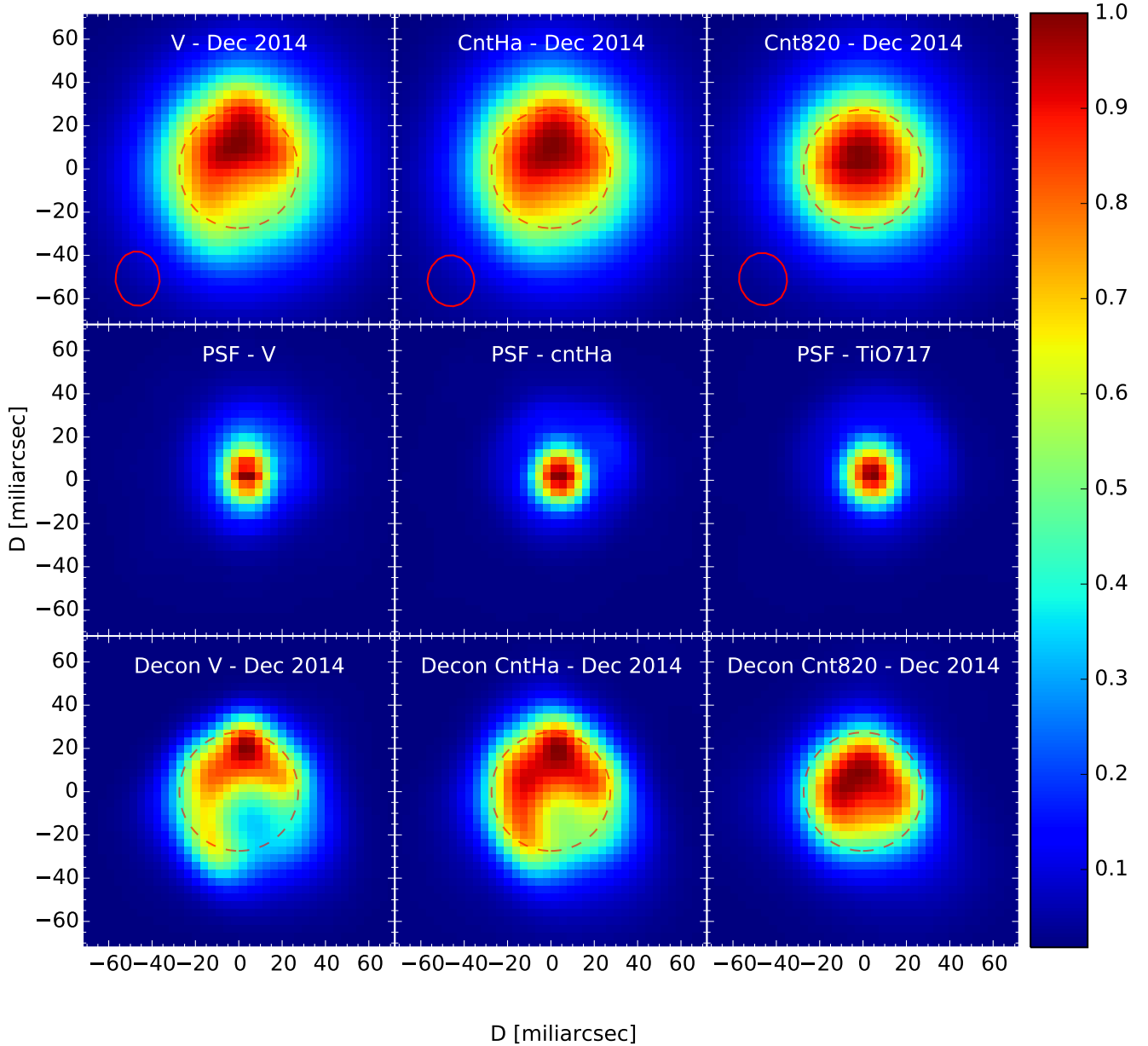


Fig. 1. *Top panels:* total intensity normalised using the peak flux as observed using ZIMPOL on 10- and 11-Dec.-2014 in the three filters, V, cntHa, and cnt820. *Middle panels:* images of the PSF-reference star ψ^2 Ori normalised to the peak flux. *Bottom panels:* corresponding deconvolved images, again normalised using the peak flux. The dashed red circles show the size of the stellar disc derived by Norris et al. (2012) from observations in the near-infrared (same as shown in Figs. 2–5). The full red circles show the FWHM of the PSF used as reference.

Table 1. Observation log.

Filter	Average JD [2 457 000+]	Exp time [min]	DIT[s] x NDIT	λ_0 [nm]	$\Delta\lambda$ [nm]	AM	θ [$''$]	$FWHM_\star$ [mas]	Peak PD [%]	MPF [%]	IPF [%]	Rem.
V – 11 Dec. 14	2.563	42.7	4×10	554.0	80.6	1.40	1.0	70.6	4.8	1.85 ± 0.15	1.25 ± 0.1	–
cntHa – 10 Dec. 14	1.767	48.0	10×4	644.9	4.1	1.40	1.35	72.1	3.0	3.15 ± 0.2	2.3 ± 0.1	–
cntHa – 28 Jan. 15	50.534	11.5	1.2×36	644.9	4.1	1.25	0.93	59.4	9.0	5.45 ± 0.9	3.6 ± 0.5	–
cnt820 – 10 Dec. 14	2.589	4.8	1.2×30	817.3	19.8	1.35	1.1	58.3	–	–	–	ND1
cnt820 – 10 Dec. 14	2.584	14.4	1.2×30	817.3	19.8	1.35	1.2	–	–	–	–	sat.

Notes. The average Julian date and the total integration time of the observations are given in Cols. 2 and 3. DIT is the exposure time of the individual frames and NDIT is the number of frames per exposure. Each cycle (DIT \times NDIT) was repeated four times to obtain $+Q$, $-Q$, $+U$, and $-U$ frames and the whole cycle was repeated several times for each filter and epoch until the total exposure time was reached. AM and θ are the airmass and the visible seeing respectively. λ_0 and $\Delta\lambda$ are the central wavelength and the FWHM of the filters used. $FWHM_\star$ is the azimuthally-averaged FWHM observed for R Dor. Peak PD, IPF, and MPF (defined in Sect. 3.2) stand, respectively, for the peak value of the polarisation degree, the integrated polarised fraction, and the maximum polarised fraction (not given for cnt820, see Sect. 2.2.2). In the last column, ND1 is the neutral density filter used and sat. indicates that the CCD is saturated.

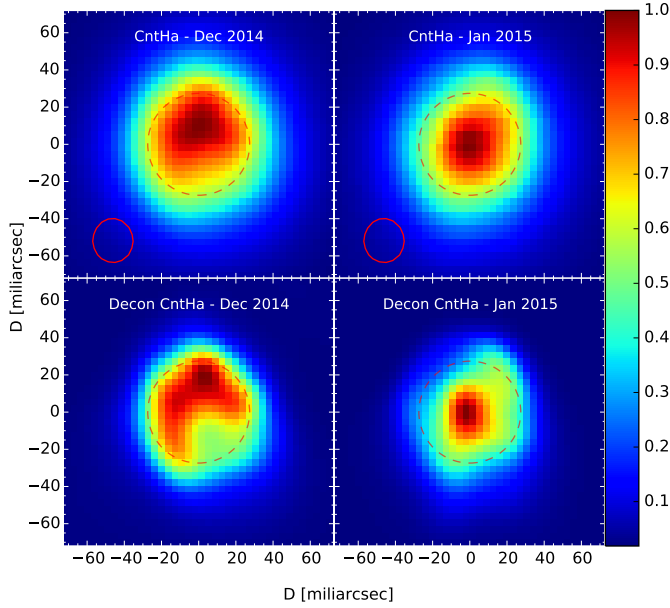


Fig. 2. *Top panels:* total intensity normalised to unity as observed using ZIMPOL in cntH α on 10-Dec.-2014 and 28-Jan.-2015. *Bottom panels:* corresponding deconvolved images, again normalised to unity. The dashed red circles show the size of the stellar disc derived by Norris et al. (2012) from observations in the near-infrared (also shown in Figs. 1–5). The full red circles show the FWHM of the PSF used as reference.

morphology are mainly caused by variability of molecular (TiO) opacity.

The variability in TiO opacity can be caused by changes in the gas density and/or in the molecular abundance or excitation. Hydrodynamical models calculated with the code CO5BOLD (Freytag 2013) for a star with a few solar masses show that convective motions can produce large-scale density variations on time scales comparable to the one we find³. However, these models lack a realistic wavelength-dependent radiative transfer that takes into account molecular opacity. As molecular excitation, and hence the surface brightness of the stellar disc, is significantly affected by density variations, by episodic dissipation of energy carried by shocks, and by variations in the stellar radiation field, a quantitative comparison between observations and such models is not yet possible.

2.2.2. The polarised light

Polarised light thought to be produced by scattering of stellar light off dust grains was detected from around the central star (see Fig. 3). The observed polarisation vectors are in the plane of the sky and tangential to a circle centred on the star, as expected for grains distributed in a circumstellar envelope illuminated by a central star. Figure 4 shows that the directions of the observed polarisation vectors match this expected behaviour up to distances of about 160 mas in the images obtained in the V filter, about 130 mas in the first-epoch cntH α image, and about 145 mas in the second-epoch cntH α image. At these radii the polarisation signal disappears in the noise. We did not include the observations in cnt820 in this analysis because these were either saturated or had to be acquired with a neutral density (ND) filter. The region where the detector was saturated includes the

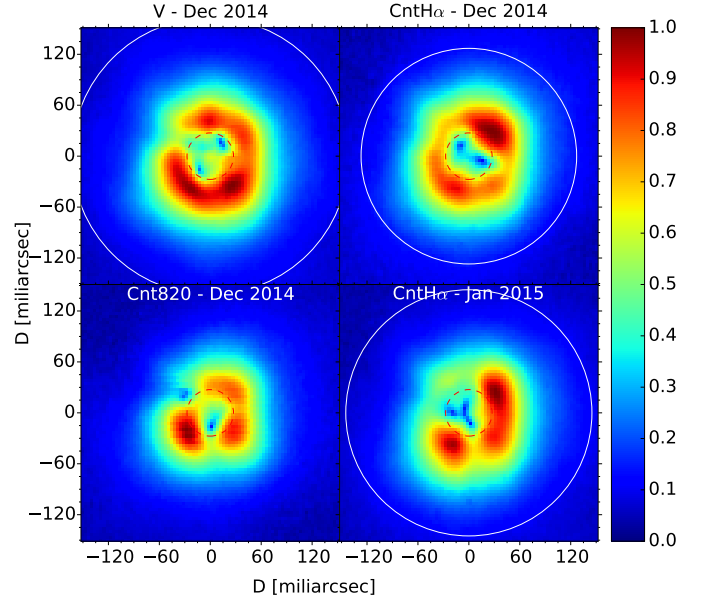


Fig. 3. Polarised intensity seen in V, cntH α , and in cnt820 on 11-Dec.-2014 and in cntH α on 28-Jan.-2015 normalised to the peak value, shown with a square-root scaling. The dashed red circles show the size of the stellar disc derived by Norris et al. (2012) from observations in the near-infrared (also shown in Figs. 1–5). The white circles (not shown for cnt820, see Sect. 2.2.2) mark the region where we find the polarised light produced in the envelope to dominate over instrumental effects.

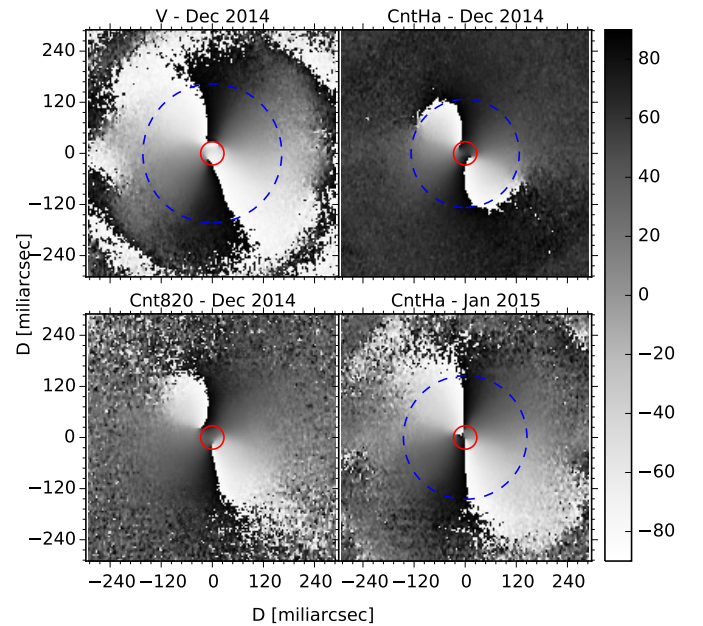


Fig. 4. Direction of the measured polarisation vector for the four images given in degrees relatively to the north direction. The red circles show the size of the stellar disc derived by Norris et al. (2012) from observations in the near-infrared (also shown in Figs. 1–3, and 5). The dashed blue circles enclose the regions where we find the polarised intensity produced in the envelope to be a factor of three larger than the expected instrumental polarisation (not shown for cnt820, see Sect. 2.2.2).

inner rim of the ring from where polarised light is seen and the ND filter can introduce uncalibrated instrumental polarisation.

The region from where we see polarised light is very similar for V and cntH α in the first epoch, but the brightness distribution is somewhat different. In V the polarised intensity is slightly more concentrated in the south part of the image (60%),

³ See <http://www.astro.uu.se/~bf/> for the model results.

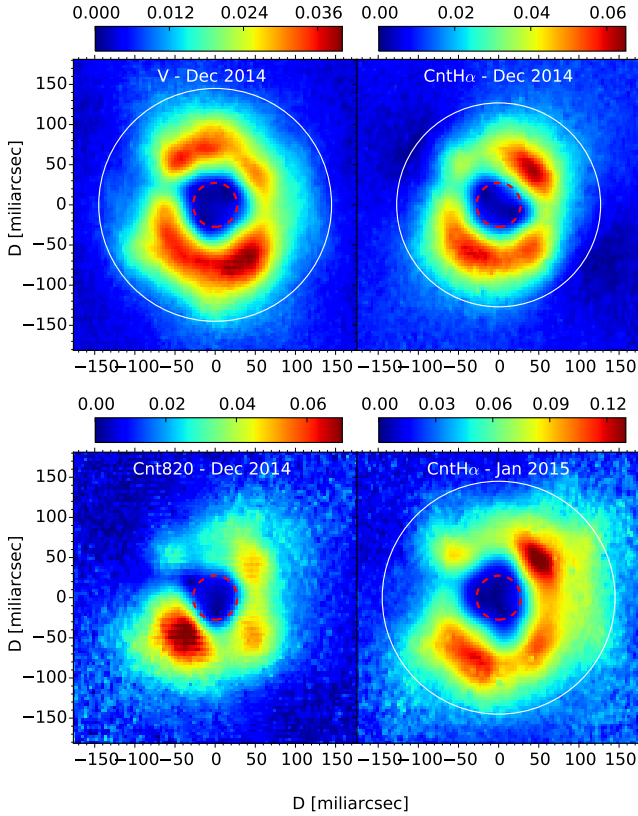


Fig. 5. Polarisation degree for the four images. The red dashed circles show the size of the stellar disc derived by Norris et al. (2012) from observations in the near-infrared (also shown in Figs. 1–4). The dashed blue circles enclose the regions where we find the polarised intensity produced in the envelope to be a factor of three larger than the expected instrumental polarisation (not shown for cnt820, see Sect. 2.2.2).

while in cntH α both hemispheres show roughly the same emission with 53% of the polarised intensity originating from the southern hemisphere. There is no obvious correlation between the directions of maximum or minimum polarised intensity and those with maximum or minimum total intensity. Interestingly, although the total intensity distribution in cntH α changes drastically from one epoch to the other, the polarised intensity distribution does not change significantly. The departure from axisymmetry is stronger in January 2015 but the location of the maxima and minima of the polarised flux does not change much between the two epochs.

We divided the image in octants to facilitate our analysis and to minimise errors introduced by asymmetries of the dust envelope. Octant 1 is limited by the north and north-east directions and the numeration follows clock-wise. The value of the polarised intensity changes considerably for the different octants. In Table 2 we list the fraction of the polarised light measured per octant per filter. The ratio between the intensity from the octants with maximum and minimum polarised intensity is roughly 2.3 for V and cntH α in the first epoch and 3.7 for cntH α in the second epoch.

3. Analysis and modelling of the polarised light

We now focus on our modelling efforts to derive the density radial profile of the grains that produce the scattered light.

Table 2. Fraction of the polarised flux arising from the different octants for the image in V and in cntH α .

Octant	Fraction of polarised flux		
	V [%]	cntH α Dec. [%]	cntH α Jan. [%]
1	11	15.5	13
2	11	13.5	16
3	13	9	14.5
4	17.5	13.5	14.5
5	16	17.5	18.5
6	13.5	13.5	11.5
7	7.5	7.5	5
8	10.5	10	7

3.1. Modelling approach

We calculated spherically symmetric models using the continuum radiative-transfer code MCMAX (Min et al. 2009). The code calculates the direction-dependent scattering of radiation by dust grains and outputs images of the Stokes parameters. We convolved the Q and U images produced by the models with the PSF images. This typically caused a decrease by a factor of 1.5 of the output integrated polarised flux. This is because in the Q and U images the negative and positive lobes from a symmetrical envelope can overlap when the resolution is lowered. This leads to polarised signal in the images to cancel out. The poorer the angular resolution, the larger is the effect. The convolved Q and U images were then combined to obtain the polarised intensity for each model.

We calculated the radial profile of the polarised intensity from the observations for each octant and compared these profiles independently to the models. We considered two different envelope structures: with dust grains distributed in a thin halo with constant density (model with no outflow), and with a dust density gradient given by $\rho(r) = \rho_0 (R_0/r)^n$, R_0 being the inner radius of the dust envelope and $\rho_0 = \rho(R_0)$. We varied R_0 between $1.2 R_\star$ and $2.0 R_\star$ for both envelope structures and the halo thicknesses between $0.25 R_\star$ and $1.5 R_\star$ for the thin-halo scenario, where $R_\star = 27.2$ mas (Norris et al. 2012).

We use amorphous Mg₂SiO₄ grains with the optical constants obtained by Jäger et al. (2003), as this dust species is one of the main candidates for driving the winds of oxygen-rich AGB stars (see, e.g., Bladh & Höfner 2012). We have also experimented with optical constants for Mg₂SiO₃ and Al₂O₃, as discussed in Sect. 4.1.2. To calculate the absorption opacities and the direction-dependent scattering properties, we approximate the actual size distribution of particle sizes by a distribution of hollow spheres (Min et al. 2003). We consider the radii, a , to be given by the standard distribution for grains in the interstellar medium $n(a) \propto a^{-3.5}$ (Mathis et al. 1977). The minimum, a_{\min} , and maximum, a_{\max} , grain radii of the distribution were varied to fit the observations (see Sect. 4.1). Our fits are only sensitive to grains with $a \gtrsim 0.1 \mu\text{m}$, since smaller grains do not provide significant scattering opacity. For distributions with $a_{\min} = 0.01 \mu\text{m}$ and a_{\max} between $0.2 \mu\text{m}$ and $0.5 \mu\text{m}$, the amount of mass in grains with $a \gtrsim 0.1 \mu\text{m}$ is roughly between 40% and 70%.

3.2. Observational constraints

Our models only consider opacity due to dust grains, while molecular absorption may also be very important close to the star. Neglecting this source of opacity will probably cause us to

overestimate the inner radius of the dust envelope. This is because photons scattered close to the star, where the gas densities are high, have a larger chance of being absorbed before escaping the envelope. Hence, the inner radius of the dust envelope would appear larger.

Instrumental polarisation may also affect the observations, though, data reduction procedures reduce it to about 0.5%. This residual instrumental polarisation mainly affects the data at projected distances >100 mas from the central source. To minimise the errors introduced, we only analysed the polarised light from the inner region up to 127 mas from the star, where the polarisation degree is larger than 1.5% and where we see the expected behaviour of the polarisation angles for the image in V and the two images in $\text{cntH}\alpha$.

We fit our models to the integrated polarised fraction (IPF), the maximum polarised fraction (MPF), and the radial profile of the polarised intensity. We define the IPF as the polarised intensity integrated within a radius of 127 mas divided by the total intensity integrated over the same region. The MPF is the maximum value of the polarised fraction per octant integrated within a radius of 127 mas divided by the total intensity integrated over a circle with a 127 mas radius. These observed quantities are given in Table 1. The errors given are the 1σ uncertainties derived from the uncertainties on the polarised intensity. We also compared our models to the radial profile of the total intensity to set upper limits on the dust densities.

The IPF in the image in V is significantly smaller than those in $\text{cntH}\alpha$ in both epochs. The polarised signal in the first-epoch $\text{cntH}\alpha$ image can be affected by the not-ideal conditions when the data were taken. Specifically, the Strehl ratio in that image is different from that in the reference PSF (ψ^2 Ori), which was taken under good sky conditions. This can cause more instrumental polarisation to be produced, affecting the IPF we measure. This is specially important in the regions where the polarisation degree is low ($\lesssim 1\%$). The effect of the worse conditions can be seen in the images of the direction of the polarisation vectors (Fig. 4). The first-epoch image in $\text{cntH}\alpha$ shows the signal from circumstellar polarisation up to a smaller distance than the second-epoch image. This would not be expected if both images had been taken under equal conditions because in the first-epoch exposure time was longer. Nonetheless, decreasing the radius of integration from 127 mas to 110 mas only reduces the value we obtain for the IPF by a factor of 1.01. Therefore, the effect of the worse sky conditions on the IPF are not significant. Moreover, the observations in January 2015 also show a high IPF in $\text{cntH}\alpha$. This leads us to conclude that the higher IPF in $\text{cntH}\alpha$ when compared to that in V is a real feature of the inner envelope of R Dor. However, we were not able to reproduce this wavelength dependence of the IPF with our models, which always show higher IPF in V or at most similar values of the IPF between the two filters.

An important consideration is that the measured IPF can be suppressed by molecular absorption. This is because the scattered photons travel longer through the envelope than photons that do not interact and, hence, have a higher probability of being absorbed by molecules. This causes the IPF produced by scattering off dust grains to decrease if the molecular absorption opacity increases in a given wavelength. Given these considerations, it is more likely that polarised photons in the V band are absorbed by molecules than artificially created in $\text{cntH}\alpha$ because of instrumental polarisation. Therefore, we consider the values measured in $\text{cntH}\alpha$ as more representative of the IPF produced by the dust. This approach also guarantees that we do not underestimate the dust densities we derive. Hence, we fit our

models to the uncertainty-weighted-averaged IPF in $\text{cntH}\alpha$ from both epochs combined, of $2.35 \pm 0.1\%$.

In order to calculate radial profiles, we need to define a central pixel but the complex morphology of the source makes this determination difficult. For reference, the FWHM of R Dor in the total intensity images in V is of roughly 20 pixels (72 mas, see Table 1). We have chosen the central pixel in the images in V as the one more closely equidistant from the peak of polarised light for different azimuths. The central pixels in the other filters were chosen by establishing the best match when overlaying the polarised-light images with those in V . By following this approach, we find that the chosen central pixels differ from the centre of light by a distance of one (3.6 mas) or two pixels (7.2 mas) for the images in V and in both epochs in $\text{cntH}\alpha$. The pixels where the total intensity peaks differ from our chosen central pixel by a distance of between 3 (10.8 mas) and 4 pixels (14.4 mas) for the image in V and the first-epoch image in $\text{cntH}\alpha$. For the second-epoch image in $\text{cntH}\alpha$, in which the stellar disc is more axisymmetric, the intensity peaks on our chosen central pixel. These considerations support our approach for determining the central pixel. The uncertainty caused by the choice of the central pixel on the derived radial profiles of the polarised intensity was taken as the maximum difference between considering the chosen central pixels or one of its eight neighbouring pixels. This approach overestimates the uncertainty on the slope of the radial profile of the polarised intensity. The effect of considering different central pixels on the IPF and MPF is negligible compared to the uncertainty of the measurements.

In Fig. 6 we compare the radial profiles for the eight octants in the images in V and in $\text{cntH}\alpha$. The profiles were normalised using the integrated polarised intensity for each filter. The radial profiles obtained from the three images are very similar and agree well within the uncertainties. The fact that the profiles from $\text{cntH}\alpha$ in the first epoch deviate slightly from the other two for $r \gtrsim 3 R_\star$ can be attributed to the worse conditions when those observations were taken and to a higher instrumental polarisation.

4. Results and discussion

We were not able to determine the particle size from the wavelength dependence of the scattering. This is because of the expected contribution of molecular opacity in the wavelength range of the observations that can disrupt the wavelength dependence imprinted by scattering. We infer that molecular opacity is important in the first epoch because of the higher IPF in V than in $\text{cntH}\alpha$, which we are not able to reproduce with our dust model.

We fit the IPF of $2.35 \pm 0.1\%$ and the radial profiles within 127 mas ($5 R_\star$, see Sect. 3.2) measured in the first epoch in V and in the second epoch in $\text{cntH}\alpha$. This means that our results are limited to a small region around the star. For reference, material moving outwards at the maximum gas expansion velocity, of 5.7 km s^{-1} , would take roughly five years to cross the region we probe. We also used the radial profile of the total intensity from the second-epoch observations in $\text{cntH}\alpha$ to set an upper limit on the dust densities allowed by the models. Finally, we investigated whether a high value of ρ_o is enough to reproduce the MPF.

4.1. The integrated polarised fraction and the radial profile of the polarised intensity

Optical-depth effects become important when we consider grain size distributions with maximum radii, a_{max} , between $0.2 \mu\text{m}$ and

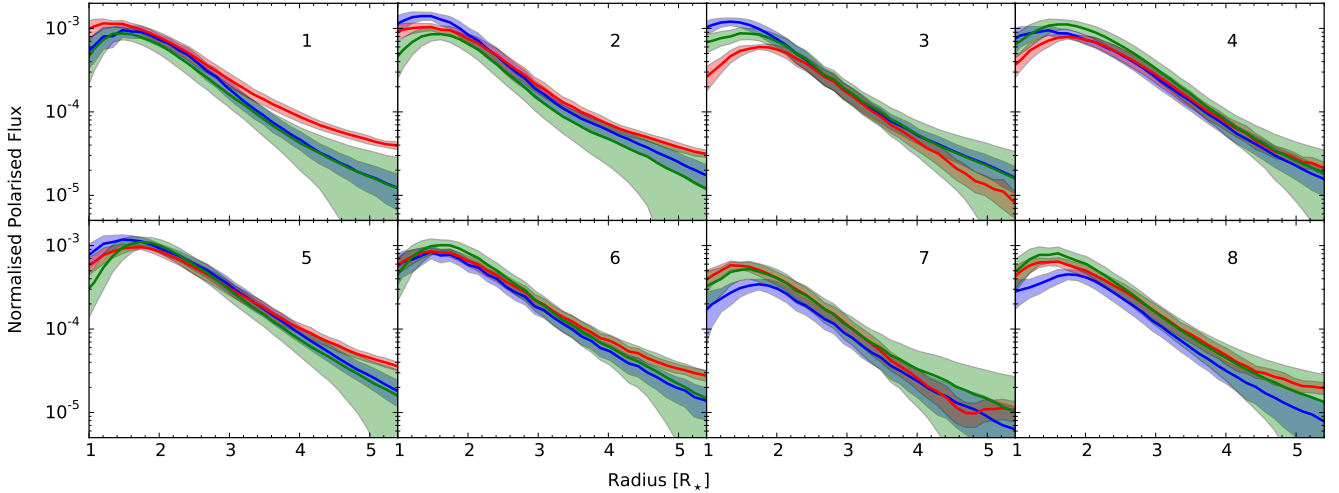


Fig. 6. Comparison between the radial profile of the polarised intensity for the different octants obtained from the observations in the first epoch in V (green line) and in $\text{cntH}\alpha$ (red line), and in the second epoch in $\text{cntH}\alpha$ (blue line). The profiles were normalised using the value of the integrated polarised intensity for each filter. The octants are identified in each panel (see Sect. 2.2.2). The filled region shows the three- σ errors from combining the uncertainty given by the ESO pipeline with that from choosing the central pixels.

$0.5\,\mu\text{m}$. For these values of a_{max} , our models require an average optical depth, $\tau_V \gtrsim 1$ to reproduce the observed IPF. In the optically-thick regime our fit parameters, ρ_o , R_o , and n cannot be determined independently.

Typically, the IPF we obtain from our models is larger than the larger the dust mass within the region of integration (127 mas). However, when $\tau_V \gtrsim 2$, increasing ρ_o , and hence the dust mass, does not lead to a larger IPF because of the effect of multiple scattering. Also, for $\tau_V \gtrsim 1.5$, the peak of the radial profile of the polarised intensity becomes broader and shifts to larger radii, in comparison to optically-thin models. This causes models with $\tau_V \gtrsim 1.5$ to require smaller values of R_o and larger values of n , when compared to optically-thin models. Our models with $\tau_V \gtrsim 1.5$ require $R_o = 1.45 \pm 0.1 R_\star$ and $3.5 \lesssim n \lesssim 5$ (with an average best-fitting value of $n \approx 4.5$) to fit the radial profile of the polarised intensity. A model with $\tau_V \approx 3.5$ requires $R_o \approx 1.2$ and $n \approx 5.5$ instead.

4.1.1. Constraints from the total intensity images

Although we do not attempt to fit the unpolarised surface brightness of R Dor, we use the radial profile of the total intensity to set an upper limit on the scattering optical depth of the envelope. The first-epoch images do not offer strong constraints because the stellar disc is seen to be very large in that epoch both in V and in $\text{cntH}\alpha$. However, as shown in Fig. 7, the second-epoch images in $\text{cntH}\alpha$ do offer important constraints. Optically-thick models overpredict the total intensity for all distances from the star. Optically-thin models also overpredict the total intensity for $r \lesssim 30$ mas but that is because our limb-darkened stellar model is not accurate enough to reproduce the brightness distribution of the stellar disc. Since the polarised fraction in $\text{cntH}\alpha$ does not seem to decrease from the first to the second epoch, we conclude that this limit on τ_V applies to both epochs. This reinforces the conclusion that the variability and asymmetries in the total intensity images in the first epoch are caused by molecular opacity. We conclude that models with scattering optical depths $\gtrsim 1.2$ do not provide acceptable fits to the data.

Moreover, the value derived by Norris et al. (2012) for the inner radius of the dust envelope of R Dor, of $R_o = 1.6 R_\star$, is in better agreement with what we obtain for models with $\tau_V \lesssim 1.5$.

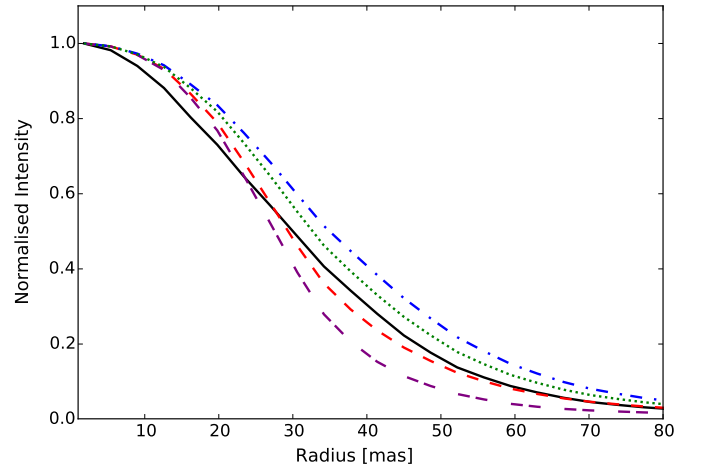


Fig. 7. Observed azimuthally-averaged radial profile of the total intensity in the second-epoch $\text{cntH}\alpha$ images (full black line) compared to models with $\tau_V = 0.65$, $R_o = 1.5 R_\star$, and $n = 4$ (dashed red line), $\tau_V = 1.3$, $R_o = 1.45 R_\star$, and $n = 4.5$ (dotted green line), and $\tau_V = 1.9$, $R_o = 1.4 R_\star$, and $n = 5$ (dotted-dashed blue line). The values of R_o and n for each of the dust models shown have been determined by fitting the radial profile of the polarised intensity. For reference, we also show the radial profile of our model star with no dust envelope (double-dashed purple line).

Since the scattering opacities in the wavelengths of the observations of Norris et al. are roughly one order of magnitude lower than those in the wavelength range of our observations, it is unlikely that their results are affected by high scattering optical depths in the envelope. This reinforces the conclusion that optically-thin models are preferred.

4.1.2. Larger grain sizes and different dust species

We have tested the effect of increasing a_{max} to values between $0.6\,\mu\text{m}$ and $1.0\,\mu\text{m}$. We find that such models produce lower values of the IPF for a given optical depth, when compared to models with smaller values of a_{max} . Therefore, the effects of high τ_V are stronger the larger a_{max} , for $a_{\text{max}} \gtrsim 0.1\,\mu\text{m}$.

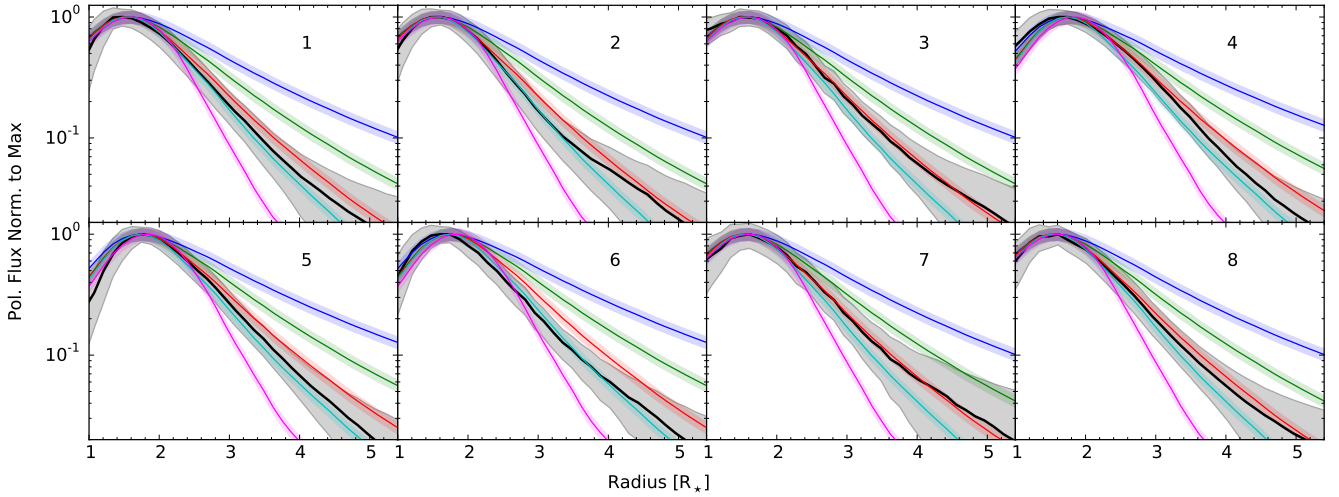


Fig. 8. Comparison between the radial profile of the polarised intensity obtained from models and from the observations in V (black line) for the different octants. Octant one is limited by the north and north-east directions and the numeration follows clock-wise. The grey-filled region shows the three- σ errors from combining the uncertainty given by the ESO pipeline with that from choosing the central pixel. The different octants are identified by number in each panel (see Sect. 2.2.2). We show the best fit models for: a thin halo (pink line), $n = 5$ (cyan line), $n = 4$ (red line), $n = 3$ (green line), and $n = 2$ (blue line). The filled regions around the model lines show variation with direction introduced by the convolution with the PSF.

Table 3. Calculated reduced- χ^2 values of the models shown in Fig. 8 fit to the radial profiles measured in the V filter for each octant.

Model	Octants							
	1	2	3	4	5	6	7	8
r^{-2}	223	194	135	184	176	226	57	172
r^{-3}	52	45	22	35	35	48	7.1	33
r^{-4}	5.8	6.4	0.63	2.2	2.5	5.3	0.27	1.6
r^{-5}	0.56	1.1	2.4	3.1	2.3	0.86	2.9	0.63
Shell	7.3	6.5	15	19	16	15	12	11

Notes. These were computed using the normalised profiles of models and observations between 18 mas and 127 mas to reflect the goodness of the fit to the shape of the observed radial profiles. The lowest reduced- χ^2 value for each octant is highlighted with boldface.

We have also experimented using optical constants for amorphous Al_2O_3 (Koike et al. 1995) and MgSiO_3 (Dorschner et al. 1995), with all other parameters kept constant. We find IPF values that differ only by a few percent from those obtained using Mg_2SiO_4 . We conclude that the effect of the assumed grain species on our results is small.

4.1.3. The radial profile of the dust density

The best-fits to the observed radial profile measured in V are shown in Fig. 8. In Table 3, we show reduced- χ^2 values for these same models fit to the normalised profile of the observed polarised flux. As can be seen, models with dust grains confined to a thin halo are not able to reproduce the observations for $r \gtrsim 2.5 R_*$, while models with $n \lesssim 3$ have dust density profiles that are too shallow and that overpredict the observed polarised intensity also for $r \gtrsim 2.5 R_*$. The dust density profiles we find are not sensitive to the size of the particles we consider, as long as the optical depth in the visual, τ_V , does not vary.

The best-fitting values of τ_V and ρ_o for models with different minimum and maximum grain sizes are given in Table 4. The dust density profiles ($n \approx 4.5$) we obtain are steeper than

Table 4. Best-fit models for the radial distribution of scattering grains using different minimum and maximum grain sizes.

a (μm)	ρ_o (g cm^{-3})	τ_V
0.01–0.05	$(3.3 \pm 1.1) \times 10^{-17}$	0.19 ± 0.07
0.01–0.1	$(6.5 \pm 2.5) \times 10^{-18}$	0.22 ± 0.08
0.01–0.2	$(1.0^{+?}_{-0.45}) \times 10^{-17}$	$1.2^{+?}_{-0.5}$
0.01–0.3	$(7.2^{+?}_{-3.4}) \times 10^{-18}$	$1.25^{+?}_{-0.6}$
0.01–0.4	$(6.0^{+?}_{-3.0}) \times 10^{-18}$	$1.10^{+?}_{-0.45}$
0.01–0.5	$(6.3^{+?}_{-3.2}) \times 10^{-18}$	$1.15^{+?}_{-0.5}$
0.3–0.5	$(3.0^{+?}_{-1.25}) \times 10^{-18}$	$1.1^{+?}_{-0.45}$

Notes. ρ_o is the density needed at R_o to produce the IPF for a model with $n = 4.5$. τ_V is the radial V-band optical depth of the corresponding model. We also show the range in ρ_o and τ_V required to reproduce the observed variation of polarisation degree between the octants with maximum and minimum values. The question marks indicate that we were not able to reproduce the MPF because the models become too optically thick.

that of a wind expanding with constant speed ($n = 2$). This can be the result of acceleration, of destruction of the dust grains in the observed region, of a decreasing mass-loss rate on short time scales, or be caused by the density structure imprinted by consecutive shock waves in the inner envelope, as predicted by 1D wind-driving models (see, e.g., Höfner et al. 2003, for gas density profiles from models for carbon-stars).

Ireland et al. (2005) observed polarised light from two low-mass-loss rate and oxygen-rich AGB stars, R Car and RR Sco, and found that the data was better reproduced by a model with a central star surrounded by a thin shell, instead of an outflow. If these sources also have steep density profiles in the inner wind, the structure they interpreted as a thin shell might actually be the edge of a dust envelope similar to that of R Dor.

Our models produce values of the scattered-light fractions in the near-infrared roughly a factor of 3.5 larger than those reported by Norris et al. (2012) for R Dor. It is not clear whether

this is caused by variability of R Dor between the times of the two observations, by systematic errors in the data acquisition methods, or by differences in the models used by us and by Norris et al. to derive these quantities.

4.2. The maximum polarised fraction

We estimated the variation in ρ_o required to reproduce the difference in the observed polarisation degree between the octants. We are not able to reproduce the MPF in cntH α (>3%) with models that have $a_{\max} \gtrsim 0.2 \mu\text{m}$ because the model envelopes become too optically thick and do not reach such high polarised fractions. By considering $a_{\max} = 0.1 \mu\text{m}$ we are able to fit the observed IPF with much lower maximum optical depths of ≈ 0.2 and we are, then, able to reproduce the MPF.

Norris et al. (2012) report grains of $0.3 \mu\text{m}$ in the outflow of R Dor. This value is in the range of grain radii for which we cannot reproduce the MPF.

4.2.1. Tangential optical depths

Given the considerable optical depths in the wavelengths we observe, asymmetries can cause tangential optical depths in the envelope to be significantly different from those in our spherically symmetrical model. The tangential optical depths are measured along the line-of-sight and in the direction of the observer between the plane of scattering and the outer edge of the envelope. For lines-of-sight with lower tangential optical depths, more polarised photons can escape. In this case, the MPF could be reproduced by an envelope with grains with $a_{\max} \gtrsim 0.2 \mu\text{m}$ and tangential optical depths varying with azimuth. In order for the polarised intensity from one octant to be a factor of 1.5 higher than that of a spherically symmetric model, the tangential optical depth would have to be 0.4 smaller. Given that the optical depths we find are of order unity, this would imply a decrease of the tangential optical depth of roughly 40% for the octants with maximum polarisation. Since the polarised fraction would depend on both the tangential optical depth and on ρ_o for each octant for non-spherically-symmetric envelopes we have not explored this possibility further.

4.3. Comparison with ZIMPOL results for W Hya

Ohnaka et al. (2016) reported SPHERE/ZIMPOL observations of the O-rich AGB star W Hya that resolved the direct stellar emission and the region in the close circumstellar environment where polarised light is produced. The authors find large grain sizes ($\sim 0.5 \mu\text{m}$) and small optical depths, of 0.1, in visual wavelengths. These are very different from our preferred models for R Dor, with optical depths in visible wavelengths of ~ 1 . Since the polarisation degree reported by Ohnaka et al. for W Hya is comparable to what we find for R Dor and the mass-loss rate of W Hya (of $\sim 1.3 \times 10^{-7} M_{\odot} \text{yr}^{-1}$, Khouri et al. 2014) is similar to that of R Dor, the differences between the results reported by Ohnaka et al. and ours are not expected.

Ohnaka et al. used a non-spherically symmetric radiative transfer model to reproduce the observations. This might affect the derived optical depths because the tangential optical depths can be considerably different from a spherically symmetric model (see Sect. 4.2.1). Moreover, the authors constrained the dust mass also taking into account the scattered light fractions reported by Norris et al. (2012) for W Hya. Therefore, the differences in the derived optical depths might be related to the

fact that we overpredict the scattered light fractions given by Norris et al. for R Dor (see Sect. 4.1.3). However, we are not able to determine the cause of these discrepancies and further investigation is needed.

We note that if our models underestimate the polarised flux for a given value of the optical depth of the envelope, the dust densities we find will be overestimated. Hence, the actual dust densities and the dust-to-gas ratio in the envelope will be smaller than the values we report.

4.4. Dust grains as wind drivers

We now investigate whether the grains we see around R Dor are sufficient for driving the wind. Wind-driving models indicate that the minimum dust-to-gas ratio (d/g) for a wind to develop is $d/g \approx 6 \times 10^{-4}$ (Höfner 2008) or even $d/g \approx 3.3 \times 10^{-4}$ (Bladh et al. 2015)⁴. These models consider grains of a single radius, which is typically $\gtrsim 0.2 \mu\text{m}$.

We estimate an empirical upper limit for the d/g at a radius r in the envelope of R Dor by considering a lower limit for the gas density, $\rho_{\text{gas}}(r) \geq \frac{\dot{M}_{\text{gas}}}{4\pi r^2 v_{\infty}}$, and the dust density profiles we find. We use the parameters commonly obtained for the gaseous outflow of R Dor of $\dot{M}_{\text{gas}} = 9 \times 10^{-8} M_{\odot} \text{yr}^{-1}$ and $v_{\infty} = 5.7 \text{ km s}^{-1}$ (see, e.g., Khouri 2014). This should give us a robust lower limit on the gas densities, since the gas expansion velocities are expected to be smaller than v_{∞} close to the star.

For the dust density profile, we use $n = 4.5$ and the average density from the model with only large grains, $\rho_o = 3 \times 10^{-18} \text{ g cm}^{-3}$, as this is the model more directly comparable to the single-grain-size models of Höfner and Bladh et al. This choice should not have a strong effect on our results because, at a given distance from the star, all our best-fitting models have densities of grains with $a \geq 0.15 \mu\text{m}$ which are always smaller or very similar to that of the model with only large grains.

We find $d/g \leq 5 \times 10^{-3}$ at $r = 1.5 R_{\star}$ and $d/g \leq 2 \times 10^{-4}$ at $r = 5.0 R_{\star}$. Although the upper limit for the d/g we derive at $r = 1.5 R_{\star}$ does not provide strong constraints, the low value for the upper limit at $r = 5.0 R_{\star}$ shows that at that radius the d/g in the outflow of R Dor is close to the limit of what wind-driving models require. We note that our results can underestimate the dust densities if the polarisation efficiency of the grains is overestimated by our model. However, this would imply higher scattering optical depths for the envelope, which our results disfavour. Given the low expansion velocity and mass-loss rate of R Dor, a low value of the d/g is not unexpected. However, if the steep radial profile of the dust density extends beyond $5 R_{\star}$, the d/g would soon become too low for the dust to provide the required opacity to drive the outflow. This would be a problem because the maximum expansion velocity of the outflow of R Dor only equals the escape velocity of a $1 M_{\odot}$ star at $r \approx 35 R_{\star}$, and hence the radiation pressure force would have to be larger than the gravitational pull up to that distance.

5. Summary and conclusions

We have observed the oxygen-rich AGB star R Dor using SPHERE/ZIMPOL on the VLT in three filters: V , cntH α , and cnt820. Observations in cntH α were acquired in two epochs 48 days apart. The stellar disc is resolved in all observations and

⁴ Both studies report silicon condensation fractions. We calculated the d/g by adopting solar silicon abundances (Asplund et al. 2009).

we are able to study asymmetries and variability in the star. We find the total intensity distribution of R Dor to have a horseshoe-shaped morphology in the first epoch both in V and in $\text{cntH}\alpha$. In the pseudo-continuum filter cnt820 the stellar disc is smaller and any departures from axisymmetry are much less pronounced. In the second-epoch, taken 48 days later, the image in $\text{cntH}\alpha$ shows a source with a very different morphology. Moreover, the stellar disc is significantly smaller than in the first-epoch image in the same filter and is comparable in size to what we see in cnt820 , also in the first epoch. We interpret these differences in size and morphology as being caused by variability in the excitation and/or density of TiO molecules in the extended atmosphere of the star.

We detect polarised light coming from a ring that encloses the central source and that spans a similar region in the three images we consider, in V and the two epochs in $\text{cntH}\alpha$. However, the polarised intensity varies significantly with azimuth for the three images and the ratio of the polarised intensity between two images also varies somewhat with azimuth. We find the integrated polarised fraction in V to be smaller than those in $\text{cntH}\alpha$ in the two epochs and the integrated polarised fraction to increase in $\text{cntH}\alpha$ from the first to the second epoch. Our fits to the integrated polarised fraction and the radial profile of the polarised intensity show that we see outflowing dust grains. Considering models with dust density profiles of the type $\rho(r) = \rho_0 r^{-n}$, we find that the dust density decreases much more steeply with radius than expected for a wind expanding at constant speed. This can be caused by the acceleration of the wind, but could also be explained by destruction of the dust grains or by a varying mass-loss rate on short time scales.

We use our best-fitting dust models and literature values for the gaseous outflow to calculate upper limits for the dust-to-gas ratio as a function of radius. We compare the limits we obtain to results from wind-driving models and we find that the upper limit we derive for the dust-to-gas ratio at $5 R_\star$ is somewhat lower than the minimum values required by such models for a wind to develop. Given the approximations we use for the grain model and the envelope structure, the upper limit we find for the dust-to-gas ratio is consistent with the value found in wind-driving models. However, if the steep dust density gradient we derive extends to larger radii, the dust-to-gas ratio would surely become too small for the outflow to be driven. Given the low expansion velocity of the outflow of R Dor, the wind only reaches the escape velocity of a one solar mass star about $35 R_\star$ from the central star. Therefore, if the grains we see are the main source of opacity that drives the wind, we would expect a flattening in the power law of the dust density profile not much farther out than the maximum radius we probe.

Further investigation of the outflow of R Dor will help to better understand how its wind is accelerated. Particularly, deeper observations using ZIMPOL can probe the dust density farther out in the envelope to better constrain the role of the scattering grains in driving the wind. Similar studies for other AGB stars will show whether what we see for R Dor is representative in any way and how the distribution of the dust in the inner wind changes for different stars. This will help advance our knowledge of the driving of AGB outflows and of the AGB evolution in general.

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